

Reminders

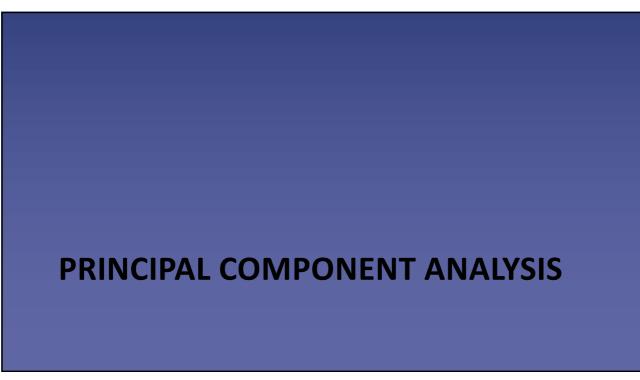
- Today we will discuss dimensionality reduction
- Next week we will have our test!



Dimensionality reduction

- In opposition to feature selection, dimensionality reduction techniques decrease the dimensionality of a problem by **combining** features
- There are different techniques to achieve this goal
- The most famous is Principal Component Analysis (PCA)





Variance and covariance

- Variance and covariance measure how "spread" a set of points are around their mean
- Variance is used for analyzing a single dimension
- Covariance measures how much each of the dimensions vary from the mean with respect to each other
- Covariance is measures between 2 dimensions to see if there is a relationship between them

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Covariance

• The covariance between 2 variables is computed by:

$$Cov(X,Y) = \frac{\sum_{i=1}^{n} (X_i - \overline{X})(Y_i - \overline{Y})}{(n-1)}$$

 If you have more than 2 variables, you need to compute a covariance matrix

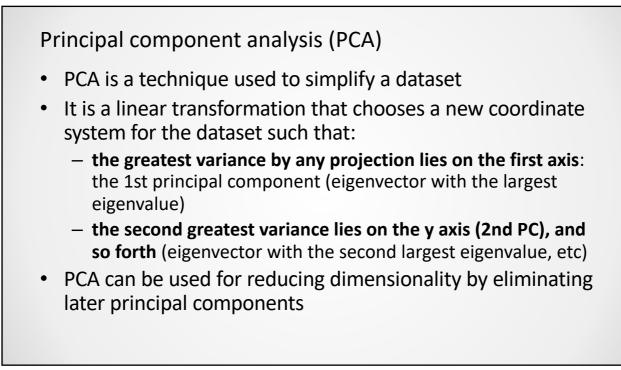
Covariance

- The exact value is not as important as its sign
- A positive value indicates both variables increase or decrease together
- A **negative** value indicates that while one variable increases, the other decreases, or vice-versa
- If covariance is **zero**, the two variables are independent from each other

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But what about correlation?

- Correlation allowed us to infere the same thing
- Why do we need covariance?
- Covariance is used to find relationships between variables in high-dimensional scenarios, where visualization is difficult



Steps to use PCA

- Normalize the data
- Calculate the covariance matrix
- Calculate the eigenvalues and eigenvectors
- Choosing principal components
- Forming a feature vector
- Forming principal components
- All but the first of these steps are covered in scikit-learn's PCA implementation

PCA Limitations

 If the data does not follow a multidimensional normal (gaussian) distribution, the principal components extracted will be distorted

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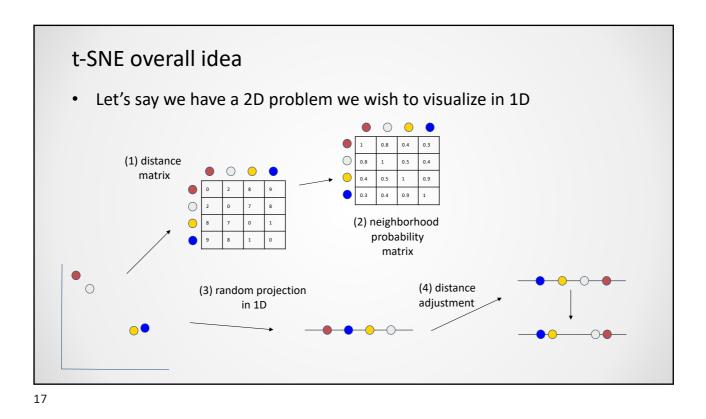
Activity

- Let's run PCA on a dataset representing customers
- Each customer represents either a restaurant, a retail store, etc
- Let's analyze its principal components



t-Stochastic Neighbor Embedding

- Technique tailored for visualizing high-dimensional datasets
- How do we visualize data in 2D or 3D?
- Two goals:
 - Distance preservation
 - Neighbor preservation
- Unsupervised, but it helps uncovering interesting aspects of the data



terms Agorithm 1: Simple version of t-Distributed Stochastic Neighbor Embedding. Data: data set $X = \{x_1, x_2, ..., x_n\}$, contraction parameters: perplexity *Perp*, optimization parameters: number of iterations *T*, learning rate η , momentum $\alpha(t)$. Result: vow-dimensional data representation $\mathcal{O}^{(T)} = \{y_1, y_2, ..., y_n\}$. For more parameters affinities $p_{j|t}$ with perplexity *Perp* (using Equation 1) set $p_{ij} = \frac{p_{ij}^{(J)} + p_{ij}}{2\pi}$ sample initial solution $\mathcal{O}^{(0)} = \{y_1, y_2, ..., y_n\}$ from $\mathcal{O}(0, 10^{-4}t)$. for t = t to *T* do (sompute [gadient $\frac{\delta C}{\delta \mathcal{O}}$ (using Equation 4) compute [gadient $\frac{\delta C}{\delta \mathcal{O}}$ (using Equation 4) $set <math>\mathcal{O}^{(1)} = \mathcal{O}^{(t-1)} + \eta \frac{\delta C}{\delta \mathcal{O}} + \alpha(t) (\mathcal{O}^{(t-1)} - \mathcal{O}^{(t-2)})$ end

